JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD M.TECH I SEMESTER EXAMINATIONS, APRIL/MAY-2012 MODERN CONTROL THEORY

$(COMMON\ TO\ ELECTRICAL\ POWER\ ENGINEERING, POWER\ ELECTRONICS)$

Time: 3hours Max.Marks:60

Answer any five questions All questions carry equal marks

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- 1. (a) Explain the advantages and disadvantages of
 - (i) physical variables
 - (ii) phase variables
 - (iii) Canonical variables for state –space formulation of control systems.
 - (b) Differential equation of dynamic system is given by

$$\ddot{c}_1 + \dot{c}_1 + 3c_1 - 5c_2 = r_1$$

 $\ddot{c}_2 + 2c_1 + c_2 = r_2$

write state equation and output equation.

- 2. (a) Derive the solution of Non-homogeneous state equations.
 - (b) Obtain the time response of the system where u(t) is the unit step function occurring at t=0.

$$\begin{bmatrix} \mathbf{x}_1 \\ \mathbf{x}_1 \\ \mathbf{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$$

- 3. (a) Explain with an example the concept of observability in continuous time invariant system.
 - (b) Consider the system given by

$$\begin{bmatrix} \mathbf{x} \\ x_1 \\ \mathbf{x}_2 \\ \mathbf{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -2 & -4 & -3 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \\ x_3(t) \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ -1 & 1 \end{bmatrix} u(t); \qquad z(t) = \begin{bmatrix} 0 & 1 & -1 \\ 1 & 2 & 1 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \\ x_3(t) \end{bmatrix}$$

Check for controllability and observability of the above system.

4. For the system represented by state equation $\dot{X}(t) = AX(t)$ the response is

$$X(t) = \begin{bmatrix} e^{-2t} \\ -2e^{-2t} \end{bmatrix} \text{ when } X(0) = \begin{bmatrix} 1 \\ -2 \end{bmatrix} \text{ ; and } X(t) = \begin{bmatrix} e^{-t} \\ -e^{-t} \end{bmatrix} \text{ when } x(0) = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

determine the System matrix A and the state transition matrix.

- 5. (a) State the Lyapunov theorems?
 - (b) Consider a non-linear system described by the equations:

$$\dot{x}_1 = -2x_1 + x_1 x_2$$
$$\dot{x}_2 = -x_2 + x_1 x_2$$

Investigate the stability about the equilibrium point $X = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$

6. A linear time invariant system is described by the state equation

$$\dot{X}(t) = AX(t) + bu(t)$$
 where

$$A = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}; b = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \qquad y(t) = \begin{bmatrix} 2 & -1 \end{bmatrix} X(t)$$

Design a state observer that makes the estimation error to decay at least as fast as e^{-10t} .

- 7. Find the optimal control $u^*(t)$ for the system $\dot{X} = \begin{bmatrix} 0 & 1 \\ -10 & 0 \end{bmatrix} X + \begin{bmatrix} 0 \\ 10 \end{bmatrix} u$ which minimizes the performance index $J = \frac{1}{2} \int_{0}^{2} u^2 dt$ Given $X(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$, $X(2) = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$
- 8. (a) What is the variable end point problem? Discuss the generalized boundary condition.
 - b) Explain the term-Linear quadratic regulator.
